

## Lecture 29

We now study the two sample problem where the data  $X_1, \dots, X_m$  iid  $\text{Normal}(\mu_1, \sigma_1^2)$  is independent of  $Y_1, \dots, Y_n$  iid  $\text{Normal}(\mu_2, \sigma_2^2)$ . Initially, we make the unrealistic assumption that both  $\sigma_1$  and  $\sigma_2$  are known.

Under the above conditions, interest lies in the unknown parameter  $\mu_1 - \mu_2$ . The test statistic used in the construction of confidence intervals and hypothesis testing is

$$\frac{\bar{X} - \bar{Y} - (\mu_1 - \mu_2)}{\sqrt{\sigma_1^2/m + \sigma_2^2/n}} \sim \text{Normal}(0, 1)$$

**Example:** Suppose that fifty test scores from class A are independent of 70 test scores from class B. Assume further that the test scores are normal,  $\sigma_1^2 = \sigma_2^2 = 84$ ,  $\bar{X} = 73$  and  $\bar{Y} = 59$ . Is there a difference between the two classes?

**Example continued: Construct a 95% confidence interval for  $\mu_1 - \mu_2$ .**

**Example continued: Suppose the question had instead been, “Is class A better than class B?”**

**Example continued: Suppose the question had instead been, “Is class A more than five marks better than class B?”**

The significance of "significance":

When we reject the null hypothesis  $H_0$ , we say that the result is *statistically significant*.

Discussion points:

- always report the p-value
- keep in mind that  $\alpha = 0.05$  is arbitrary
- significance does not always mean importance
- p-values are related to sample size

More on stat significance vs practical importance:

Example: Spring Birthday Confers Height Advantage - Yahoo Health News, Feb 18/98

In an Austrian study of 507,125 military recruits, it was found that the average height of those born in the spring was  $1/4$  inch more than those born in the fall.